## Problem 1.20

Find  $V_o$  and the power absorbed by each element in the circuit of Fig. 1.31.



## Solution

To get the power for a circuit element, multiply the voltage and current through it. The current is negative if it flows out of the element through the positive end.

 $p_{\text{independent voltage source}} = (30 \text{ V})(-6 \text{ A}) = -180 \text{ W (emitted})$   $p_{\text{left 12 V}} = (12 \text{ V})(6 \text{ A}) = 72 \text{ W (absorbed})$   $p_{\text{middle } V_0} = (V_0)(3 \text{ A}) = 3V_0 \text{ W (absorbed})$   $p_{\text{right 1 A}} = (28 \text{ V})(1 \text{ A}) = 28 \text{ W (absorbed})$   $p_{\text{right 2 A}} = (28 \text{ V})(2 \text{ A}) = 56 \text{ W (absorbed})$   $p_{\text{dependent voltage source}} = (5 \times 2 \text{ V})(-3 \text{ A}) = -30 \text{ W (emitted})$ 

Use the fact that the sum of power in this circuit is zero (law of conservation of energy) to solve for  $V_0$ .

$$\sum p = (-180 + 72 + 3V_0 + 28 + 56 - 30) \text{ W} = (3V_0 - 54) \text{ W} = 0$$

Therefore,

$$V_0 = 18 \text{ V} \implies p_{\text{middle } V_0} = 3V_0 = 54 \text{ W}.$$